APMA 1650 – Review Session 1

Friday, July 8, 2016

Some of the problems I will go over in the review session are from the recitation sheet. Here are some other problems.

- 1. You have 5 different and distinguishable pairs of socks in your drawer. If you randomly select four socks from the drawer, what is the probability that there is no matching pair?
- 2. Suppose we have a group of 22 high school students. We will divide them into two teams of 11 to play soccer.
 - (a) If we divide them into a JV (junior varsity) and varsity team, how many ways are there to do this.
 - (b) If we divide them into two soccer teams, how many ways are there to do this?
- 3. At a certain intersection, the a traffic light is red for 15 seconds, yellow for 5 seconds, and green for 30 seconds.
 - (a) Find the probability that out of the next 10 cars which arrive randomly at the light, exactly 4 will be stopped by a red light.
 - (b) What is the expected number of the next 10 cars which will be stopped by the light. What is the variance?
- 4. A bag contains 20 marbles; 5 are red and 15 are white. You draw marbles from the bag one at a time, replacing them after each draw.
 - (a) If you make 10 draws from the bag, what is the probability that fewer than 3 of them will be red?
 - (b) What is the expected value and variance of the number of red balls drawn out of 10?

Now suppose you keep drawing from the bag (with replacement) until you get a red ball.

- (c) What is the probability that you will get a red ball on the first 3 draws?
- (d) What is the probability that it takes longer than 10 draws to get a red ball?

- (e) What is the expected value and variance of the number of draws it takes to get the first red ball?
- 5. Suppose I make an average of 2 spelling mistakes per page in my class notes. Modeling this with an appropriate probability distribution, what is the probability that any given page has 2 or fewer spelling mistakes on it?