APMA 0350 – HOMEWORK 4

Problem 1: (5 points)

Apply Euler's method by hand with N = 4 to find y_0, y_1, y_2, y_3, y_4 on [0, 1] where

$$\begin{cases} y' = -2y + 3t\\ y(0) = 1 \end{cases}$$

Note: Please don't use Python for this. You **are** allowed to use a calculator do the arithmetic and to use approximate values.

Problem 2: (5 = 3 + 2 points) Solve the following **exact** ODE. Leave your answer in implicit form. Don't forget to check for exactness

(a)

$$\frac{dy}{dx} = -\left(\frac{e^x \sin(y) - 2y \sin(x)}{e^x \cos(y) + 2\cos(x)}\right)$$
(b)

$$\frac{dy}{dx} = -\left(\frac{e^x \sin(y) - 2y \sin(x)}{e^x \cos(y) + 2\cos(x)}\right)$$

 $\frac{dg}{dx} = -\left(\frac{f(x)}{g(y)}\right)$ **Note:** Your answer will involve antiderivatives F and G of f and g respectively. This shows that exact equations are more general than separation of variables.

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Problem 3: (5 = 2 + 2 + 1 points)

Find the general solution of the following ODE:

(a) y'' = y' + y (this involves a number called the golden ratio)

(b)
$$6y'' - 7y' + 2y = 0$$

(c) An ODE whose auxiliary equation is

$$(r-1)r(r+1)(r+2) = 0$$

Problem 4: (5 points) Solve the following ODE

$$\begin{cases} y'' - 3y' - 28y = 0\\ y(0) = 3\\ y'(0) = -1 \end{cases}$$