# Probing the BFKL dynamics at hadronic colliders

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Contents:

- Forward jets at HERA
- Mueller Navelet jet
- Jet veto (atlas measurement)
- Jet gap jet at Tevatron, LHC
- Jet gap jet in diffraction at the LHC

Work done in collaboration with D. Werder, O. Kepka, C. Marquet, R. Peschanski, M. Trzebinski, Y. Hatta, G. Soyez, T. Ueda

- Forward jets: Nucl. Phys. B 739 (2006) 131; Phys. Lett. B 655 (2007) 236; Eur. Phys. J. C55 (2008) 259;
- Mueller Navelet jets: Phys. Rev. D79 (2009) 034028;
- Jet Gap Jet: Phys. Rev. D79 (2009) 094019; Phys.Rev. D83 (2011) 034036; Phys. Rev. D 87 (2013) 034010
- Jet veto: Phys.Rev. D87 (2013) 054016



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- Full BFKL NLL calculation used for the BFKL kernel, available in S3 and S4 resummation schemes to remove the spurious singularities (modulo the impact factors taken at LL)
- Equation:

$$\frac{d\sigma_{T,L}^{\gamma^* p \to JX}}{dx_J dk_T^2} = \frac{\alpha_s(k_T^2)\alpha_s(Q^2)}{k_T^2 Q^2} f_{eff}(x_J, k_T^2)$$
$$\int \frac{d\gamma}{2i\pi} \left(\frac{Q^2}{k_T^2}\right)^{\gamma} \phi_{T,L}^{\gamma}(\gamma) \ e^{\bar{\alpha}(k_T Q)\chi_{eff}[\gamma, \bar{\alpha}(k_T Q)]Y}$$

• Implicit equation:  $\chi_{eff}(\gamma, \alpha) = \chi_{NLL}(\gamma, \alpha, \chi_{eff}(\gamma, \alpha))$  solved numerically

#### **Comparison with H1 triple differential data**



d  $\sigma/dx dp_T^2 d Q^2$  - H1 DATA

#### **Mueller Navelet jets**

Same kind of processes at the Tevatron and the LHC



- Same kind of processes at the Tevatron and the LHC: Mueller Navelet jets
- Study the  $\Delta\Phi$  between jets dependence of the cross section:

## Mueller Navelet jets: $\Delta \Phi$ dependence

- Study the  $\Delta\Phi$  dependence of the relative cross section
- Relevant variables:

$$\Delta \eta = y_1 - y_2$$
  

$$y = (y_1 + y_2)/2$$
  

$$Q = \sqrt{k_1 k_2}$$
  

$$R = k_2/k_1$$

• Azimuthal correlation of dijets:

$$\frac{2\pi \left(\frac{d\sigma}{d\Delta\eta dR d\Delta\Phi}\right)}{\frac{d\sigma}{d\Delta\eta dR}} = 1 + \frac{2}{\sigma_0(\Delta\eta, R)} \sum_{p=1}^{\infty} \sigma_p(\Delta\eta, R) \cos(p\Delta\Phi)$$

where

$$\sigma_p = \int_{E_T}^{\infty} \frac{dQ}{Q^3} \alpha_s (Q^2/R) \alpha_s (Q^2R)$$
$$\left(\int_{y_<}^{y_>} dy x_1 f_{eff}(x_1, Q^2/R) x_2 f_{eff}(x_2, Q^2R)\right)$$
$$\int_{1/2-\infty}^{1/2+\infty} \frac{d\gamma}{2i\pi} R^{-2\gamma} e^{\bar{\alpha}(Q^2)\chi_{eff}(p)\Delta\eta}$$

#### Mueller Navelet jets: $\Delta \Phi$ dependence

•  $1/\sigma d\sigma/d\Delta \Phi$  spectrum for BFKL LL and BFKL NLL as a function of  $\Delta \Phi$  for different values of  $\Delta \eta$ , scale dependence: ~20%



#### Effect of energy conservation on BFKL equation

- BFKL cross section lacks energy-momentum conservation since these effects are higher order corrections
- Following Del Duca-Schmidt, we substitute  $\Delta\eta$  by an effective rapidity interval  $y_{eff}$

$$y_{eff} = \Delta \eta \left( \int d\phi \cos(p\phi) \frac{d\sigma^{O(\alpha_s^3)}}{d\Delta \eta dy dQ dR d\Delta \Phi} \right)$$
$$\left( \int d\phi \cos(p\phi) \frac{d\sigma^{LL-BFKL}}{d\Delta \eta dy dQ dR d\Delta \Phi} \right)^{-1}$$

where  $d\sigma^{O(\alpha_s^3)}$  is the exact  $2 \rightarrow 3$  contribution to the  $hh \rightarrow JXJ$  cross-section at order  $\alpha_s^3$ , and  $d\sigma^{LL-BFKL}$  is the LL-BFKL result

• To compute  $d\sigma^{O(\alpha_s^3)}$ , we use the standard jet cone size  $R_{cut} = 0.5$  when integrating over the third particle's momentum

#### Mueller Navelet cross sections: energy conservation effect in BFKL

- Effect of energy conservation on BFKL dynamics
- Large effect if jet  $p_T$  ratios not close to 1: goes closer to DGLAP predictions, needs jet  $p_T$  ratio < 1.1-1.15





- Select events with two high  $p_T$  jets, well separated in rapidity by  $\Delta y$
- Veto on additional jet activity (with  $k_T > Q_0$ , with  $Q_0 \gg \Lambda_{QCD}$ ) between the two jets
- Measure the "gap" fraction: dijet events with jet veto / total dijet events

## **Comparison with QCD calculation**



 The standard NLO and parton shower approach (POWHEG + pythia or herwig) fails to describe data

$$\frac{(d\sigma^{2\to 2} + d\sigma^{2\to 3})_{p_{T_3} < E_{out}}}{d\sigma^{2\to 2} + d\sigma^{2\to 3}}$$

- BFKL resummation (HEJ Monte Carlo) also fails to describe data
- Both approaches miss the resummation of soft gluons at large angles

#### Gluon emission at large angles



- Resummation of soft gluon emissions at large angle not taken into account in parton showers
- Resummation of soft emissions performed in  $e^+e^-$  case: when  $p_T \gg E_{out}$ , one can resum the soft logarithms  $(\alpha_S \log p_T / E_{out})^n$  while requiring that the energy flow into the region between the jets is less than  $E_{out}$

# Banfi Marchesini Smye equation



• Compute the probability  $P_T$  that the total energy emitted outside the jet cone is less than  $E_{out}$ 

• Numerical solutions are available (Hatta and Ueda, 2009)

#### **Comparison with ATLAS data**



- Good agreement between prediction and ATLAS data (black points when the most forward and backward jets are selected and E<sub>out</sub>=20 GeV)
- Plot as a function of  $\Delta y$  between jets in different jet  $p_T$  bins
- Green band: renormalisation and factorisation scale uncertainties (between  $2p_T$  and  $p_T/2$ ); yellow band: uncertainties related to sub-leading logs

#### **Comparison with ATLAS data**



- Good agreement between prediction and ATLAS data (black points when the most forward and backward jets are selected and E<sub>out</sub>=20 GeV)
- Plot as a function of jet  $p_T$  in different  $\Delta y$  bins
- Measurement not sensitive to BFKL effects

### Jet gap jet cross sections



- Test of BFKL evolution: jet gap jet events, large  $\Delta \eta$ , same  $p_T$  for both jets in BFKL calculation
- Principle: Implementation of BFKL NLL formalism in HERWIG Monte Carlo (Measurement sensitive to jet structure and size, gap size smaller than  $\Delta \eta$  between jets)

#### **BFKL formalism**

• BFKL jet gap jet cross section: integration over  $\xi$ ,  $p_T$  performed in Herwig event generation

$$\frac{d\sigma^{pp \to XJJY}}{dx_1 dx_2 dp_T^2} = S \frac{f_{eff}(x_1, p_T^2) f_{eff}(x_2, p_T^2)}{16\pi} \left| A(\Delta \eta, p_T^2) \right|^2$$

where S is the survival probability (0.1 at Tevatron, 0.03 at LHC)

$$A(\Delta \eta, p_T^2) = \frac{16N_c \pi \alpha_s^2}{C_F p_T^2} \sum_{p=-\infty}^{\infty} \int \frac{d\gamma}{2i\pi} \frac{[p^2 - (\gamma - 1/2)^2]}{[(\gamma - 1/2)^2 - (p - 1/2)^2]}$$
$$\frac{\exp\left\{\frac{\alpha_s N_C}{\pi} \chi_{eff} \Delta \eta\right\}}{[(\gamma - 1/2)^2 - (p + 1/2)^2]}$$

- $\alpha_S$ : 0.17 at LL (constant), running using RGE at NLL
- BFKL effective kernel  $\chi_{eff}$ : determined numerically, solving the implicit equation:  $\chi_{eff} = \chi_{NLL}(\gamma, \bar{\alpha} \ \chi_{eff})$
- S4 resummation scheme used to remove spurious singularities in BFKL NLL kernel
- Implementation in Herwig Monte Carlo: needed to take into account jet size and at parton level the gap size is equal to  $\Delta \eta$  between jets
- Herwig MC: Parametrised distribution of  $d\sigma/dp_T^2$  fitted to BFKL NLL cross section (2200 points fitted between  $10 < p_T < 120$  GeV,  $0.1 < \Delta \eta < 10$  with a  $\chi^2 \sim 0.1$ )

#### **BFKL** formalism: resummation over conformal spins

- Study of the ratio  $\frac{d\sigma/dp_T(all \ p)}{d\sigma/dp_T(p=0)}$
- Resummation over p needed: modifies the  $p_T$  and  $\Delta \eta$  dependences...:



#### **Comparison with D0 data**

- D0 measurement: Jet gap jet cross section ratios as a function of second highest E<sub>T</sub> jet, or Δη for the low and high E<sub>T</sub> samples, the gap between jets being between -1 and 1 in rapidity
- Comparison with BFKL formalism:

$$Ratio = \frac{BFKL \ NLL \ Herwig}{Dijet \ Herwig} \times \frac{LO \ QCD \ NLOJet + +}{NLO \ QCD \ NLOJet + +}$$

• Reasonable description using BFKL NLL formalism



# **Predictions for the LHC**

- Weak  $E_T$  and  $\Delta \eta$  dependence
- Large differences in normalisation between BFKL LL and NLL predictions



# Jet gap jet events in diffraction

- Study BFKL dynamics using jet gap jet events
- Jet gap jet events in DPE processes: clean process, allows to go to larger  $\Delta\eta$  between jets
- See: Gaps between jets in double-Pomeron-exchange processes at the LHC, C. Marquet, C. Royon, M. Trzebinski, R. Zlebcik, ArXiv:1212:2059, accepted by Phys. Rev. D





# Jet gap jet events in diffraction

- Measure the ratio of the jet gap jet to the dijet cross sections: sensitivity to BFKL dynamics
- As an example, study as a function of leading jet  $p_T$
- Advantage: ratio close to 10% (no survival probability), very clean events since jets not "polluted" by remnants)



## **Conclusion**

- Full implementation of BFKL NLL kernel for many jet proceeses at HERA, Tevatron and LHC
- Forward jets at HERA: DGLAP NLO fails to describe HERA data, good description of data using BFKL NLL formalism
- Mueller Navelet jets: Larger decorrelation expected for BFKL formalism, unfortunately suffers a lot of corrections intriduced when ones imposes the conservation of energy in the BFKL formalism (see Phys. Rev. D79 (2009) 034028)
- Jet veto measurements in ATLAS: related to QCD radiation outside jets, not to BFKL resummation effects
- Jet gap jets:
  - NLL BFKL cross section implemented in HERWIG
  - Fair description of D0 and CDF data
  - Jet gap jet events in diffraction to be measured at the LHC

# Parenthesis: LHC Forward Physics Working Group

- Motivation: New working groups aim at producing a strong physics case to be used within each experiment and in front of LHCC
- Aim: Common strategy between the different experiments and common requests to the LHC (special runs...)
- New detectors to be added (forward proton detectors, scintillators for a better coverage in rapidity...), better understanding of the forward region...
- Web page location: http://lpcc.web.cern.ch/lpcc/index.php?page=fwd\_wg under the LPCC series of working groups (Michelangelo Mangano); meetings are anounced, twiki to be built
- If interested, please register at: http://simba3.web.cern.ch/simba3/SelfSubscription.aspx? groupName=lhc-fwdlhcwg
- The final output (April-May 2014) will be a CERN yellow report submitted to the LHCC: theory, phenomenology, simulation results

# LHC Forward Physics Working Group

- New physics or topics related to searches (mostly high lumi):
  - Understanding underlying events (forward detectors)
  - Central exclusive production (jets, Higgs..) with proton tagging
  - Electroweak vector scattering ( $\gamma \gamma \rightarrow WW$ , anomalous coupling)
- Understanding the Standard model (QCD)
  - Totem/Alfa: total cross section, elastic scattering, soft diffraction
  - BFKL : jet-gap-jet, hard color singlet exchange; Mueller-Navelet jets)
  - Single hard diffraction
  - Monte Carlo in forward direction, including rapidity gaps
  - Double Pomeron with hard scale (inclusive, Pomeron structure function)
  - Gamma-Pomeron, with and without hard scale
  - Drell-Yan in the forward direction (small-x, saturation)
  - pA and AA: saturation, CGC
  - Shower development and Cosmic Ray: LHCf and forward proton fragmentation
  - Role of light mass state in Exclusive production

# Working groups and conveners

- Chair: Nicolo Cartiglia (CMS), Christophe Royon (ATLAS)
- Steering group with representants from all LHC experiments
- Three different working groups:
  - "Low" luminosity (up to a few 10 pb<sup>-1</sup>); Lucian Harland Lang (theory, Co-chair), Valery Khoze (theory), Martin Poghosyan (Alice), Tim Martin (ATLAS, Co-chair), Antonio Vilela (CMS), Dima Volyanskyy (LHCb), Takashi Sako (LHCf), Alessia Tricomi (LHCf), Valentina Avati (Totem)
  - "Medium" luminosity (up to a few 100 pb<sup>-1</sup>); Cyrille Marquet (theory), Jochen Bartels (theory, Co-chair), Gerardo Herrera (Alice), Christophe Royon (ATLAS), Nicolo Cartiglia (CMS), Ronan McNulty (LHCb), Paula Collins (LHCb, Co-chair), Ken Osterberg (TOTEM)
  - "High" Luminosity (a few 100 fb<sup>-1</sup>); Rikard Enberg (theory), Antoni Szczurek (theory Co-chair), Jonathan Hollar (CMS, Co-chair), Risto Orava (TOTEM), Rafal Staszewski (Atlas)

# Working Group Meetings

- 2 day meetings every 4-5 weeks (longer for meetings outside): half day for each working group, 1 half day for common sessions and summary of the 3 working group activities
- May 15-16: CERN
- July 15-18: Reggio de Calabria, Italy, please register at http://www-d0.fnal.gov/ royon/diffraction\_calabria; preliminary agenda from working groups by mid-June, final version by 1st week of July; 1 day per WG
- August 26-27: CERN
- October 16-17: CERN
- November 18-19-20: Cracow
- January 14-15: CERN
- Last week of February 1st week of March: CERN
- End of April?: Trento (tbc)